FINAL REPORT

FOR

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ATMOSPHERE AND WIND MODELING FOR ATC

PRINCIPAL INVESTIGATOR:

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1. Atmospheric Modeling

Pressure, temperature and density of the atmosphere vary considerably with altitude, and in addition, exhibit additional spatial and temporal variations. Since aircraft motions and sensors are highly dependent on these atmospheric properties, it is important to understand and to model these variations in the development of an ATC advisory scheme. In this section we review briefly the concept of the model atmosphere, and how this model should be corrected to allow for real variations.

1.1 The Model atmosphere

To predict the gross pressure and density properties of the atmosphere at typical aircraft altitudes, it is sufficient to model the atmosphere as a perfect gas, and as a fluid in equilibrium on a non-rotating, flat earth. Such a fluid satisfies:

- (1) Perfect gas law: $p = \rho RT$
- (2) The hydrostatic equation: $dp = -\rho g dh$ where p, ρ , T are the pressure, density and temperature respectively, R is the gas constant (Universal gas constant R* divided by the molecular weight of air) and h is the geometric altitude measured positive upwards.

To determine the atmosphere completely, one additional relation between these variables is required. In a theoretical sense this should be a thermodynamic equation expressing conservation of energy; that is the heat balance between internal energy, and heat flux through radiation, conduction and convection. This last relationship is difficult to express; instead, for the purposes of defining an "average" atmosphere, an average temperature variation with altitude is assumed, and this together with equations (1)-(2) define the model atmosphere.

Various atmospheric models have been proposed and are in use. The most common and universally used is the ICAO (International Civil Aviation Authority) which was introduced in 1952 to cover altitudes up to 20km (approximately 65,500ft). The ICAO atmosphere is similar to, but supercedes, the NACA (National Advisory Committee for Aeronautics) atmosphere developed in the United States and the ICAN (International Commission for Aerial Navigation) atmosphere developed in Europe. Since 1952 this atmosphere has been refined to cover altitudes up to satellite levels but the levels up to 20km are essentially unchanged. (See, for example, the US Standard Atmosphere, 1962[1]) This atmosphere is a statistical average over the year for mid-latitudes in the northern hemisphere.

In the altitude range of interest the temperature is defined by two linear functions which define two atmospheric regions:

a) Troposhere:

0 < h < 11 km T = 288.15 - 0.0065h (deg K)

b) Stratosphere:

11km < h T= 216.65 (deg K)

The mean temperature at the earth surface is 288.15 K - 15 C - 59 F - 518.67 R . The slope of the temperature versus altitude curve is referred to as the lapse rate and in the troposphere has the defined value -0.0065 deg C/m (or -0.00367 deg F/ft). The stratosphere is modeled as an isothermal region at a temperature of -56.5 deg C (216.65 K) or -69.7 deg F (389.97 deg R). The dividing line between the troposphere and the stratosphere is referred to as the tropopause and in the model atmosphere is defined at 11km - 36089ft (commonly rounded off to 36,000ft). The pressure at sea level (h=0) is defined in the model atmosphere to be exactly $p_0 = 1.013250$ 10^5 newtons/m² = 1013.25mbar. This corresponds to 760mm Hg or approximately 29.92 in Hg. In English units the pressure is 2116.22psf.

Using this assumed temperature profile the pressure and density can be easily generated by integration. The analytical expressions are given by:

$$p/p_0 = [1 + \alpha h/T_0]^{-n}$$
 h < 11km

$$p/p_{11} = \exp[-(h - h_{11})/h_{s}]$$
 h > 11 km

where p_0 is the assumed pressure at sea level (1013.25 mb)

 $n = g/\alpha R = 5.25588$

 $h_s = RT/g = 6.3416km = 20,610ft (scale height)$

 p_{11} = 226.321 mb (Calculated pressure at 11 km)

 h_{11} = 11km = 36089ft (Tropopause altitude)

One additional note is that in the model atmosphere the gravitational constant 'g' is taken to be constant in all equations and is defined as g = 9.80665 m/s². In fact, g varies with altitude (as well as with latitude), hence the resultant altitude in the model atmosphere is referred to as 'geopotential altitude' and is not the geometric (or physical) altitude. Since 'g' decreases with altitude, the geopotential altitude will be slightly less than the geometric altitude. The relation between geometric altitude and geopotential altitude is easily derived (See Ref. 1) but for the altitudes covered by commercial air traffic the difference between these two is considered insignificant. (At the tropopause the difference is about 60ft.) In this report no distinction is made between geopotential and geometric altitudes.

1.2 Atmospheric Variations

Obviously there are few 'average' days where the temperature profile exactly matches the profile assumed in the model atmosphere. Also surface pressure is highly variable from the standard value although percent deviations are smaller than those in temperature. Surface temperatures in

particular exhibit considerable variation from 15 deg C, but even at higher altitudes temperatures may deviate significantly from the model values. Figure 1, taken from Reference 1, depicts the historically observed statistical variations of atmospheric density and temperature. These fluctuations are large enough to have a significant effect on aerodynamic and thrust forces on an aircraft, hence consideration of an accurate ambient atmospheric is necessary for accurate trajectory prediction.

The effect on aircraft performance is felt several ways. Since an aircraft altimeter is calibrated to translate pressure into an altitude reading based on the model atmosphere (see Section 1.4), the aircraft altimeter will not read the true geometric altitude. Nor will the calibrated airspeed measured in the cockpit, have the standard relationship to true airspeed due to an implicit temperature dependency. Engine performance will be different than expected since the air density and temperature are different from the standard values. Finally, wind errors will be introduced because of the difference between true altitude and the altimeter reading. What this translates to is that uncertainty in the temperature profile can be a major source of error in the prediction algorithms which determine expected landing times based on standard descent procedures.

1.3 Incorporation of Actual Atmospheric Data into CTAS

One of the primary elements of the CTAS (Center/Tracon Advisory System) software being developed by NASA is the trajectory prediction component which takes aircraft entering into the center advisory region and calculates

precise trajectories to touchdown. Key to the success of the CTAS system is its ability to project the arrival times at various waypoints so as to ensure smooth uninterrupted flow through the system. To ensure the accuracy of such a system two components are needed: 1) An accurate database of aircraft types, force coefficients and aerodynamic data, and 2) accurate atmospheric models with requisite spacial and temporal fidelity. One component of this atmospheric model is the accurate knowledge of pressure, temperature and density in the atmosphere. Another is the problem of determining accurate wind information which is discussed in the next section.

From the previous section it is obvious that the atmospheric parameters are determined by the surface pressure and the variation of temperature with altitude. This latter requirement causes difficulty since often only surface temperatures are available. Standard correction procedures advocated for use by pilots use the standard lapse rate of the model atmosphere, coupled with surface temperature data, to compute density and true altitude variations from the pressure altitude, or altimeter reading. (See e.g. Ref.2) This may also include either an adjustment of the tropopause height or an adjustment of the stratosphere temperature. Such corrections however may be significantly in error, since surface conditions are quite variable, and do not always reflect upper atmosphere changes. This is especially true for high altitude airports, such as Denver's Stapleton Airport which is above 5000ft. The model atmosphere temperature at this height is 5 deg C (41 deg F) while surface temperatures of 90 deg F are quite common in Summer. Projecting temperature variations at upper

altitudes based on this number alone introduces the possibility of significant errors. Even if surface pressure is 'standard', temperature deviations from standard values in the vicinity of the surface can introduce significant differences between the 'pressure altitude' (i.e. the altitude corresponding to a pressure level in the standard atmosphere) and the true altitude at much higher altitudes. Figure 2a shows a temperature profile which deviates from the standard in the altitude range from 0-5000ft, then follows the model atmosphere temperature profile above 5000ft. Assuming the surface pressure is standard the deviation between the pressure altitude and the geometric altitude is shown on Figure 2(b). For this profile peak altitude deviations are about 1500 ft.

If no high altitude temperature data is available, then some apriori modeling procedure is clearly necessary. If however additional temperature data is available, as, for example, from descending or ascending aircraft, then these temperature variations can easily be included into an accurate atmospheric model.

1.4 Implementation of an Atmosphere model for CTAS

In this section we assume that a temperature profile and the surface pressure in the atmosphere are known. What we detail here is how to implement this into the CTAS algorithms. We assume that temperature is known at a series of altitudes (h_i, T_i) , i=1,n. Then assuming a linear temperature variation between points, the pressure and temperature profiles are:

$$(T/T_{i}) = 1 + \alpha_{i}(h - h_{i})/T_{i}$$

$$p/p_i = (T/T_i)^{-g/\alpha}i^R$$

for $h_i < h < h_{i+1}$ and where

$$\alpha_{i} = \frac{T_{i+1} - T_{i}}{h_{i+1} - h_{i}}$$
 $i = 1, ..., n-1$

At the last point h_n , T_n , or if α_i = 0, (that is,if the atmosphere is locally isothermal) the pressure relation above is replaced by the exponential form

$$p/p_i = \exp(-g(h - h_i)/RT_i)$$

Our procedure then is to sequential compute the temperature and pressure at the interface between successive layers, and to store the atmospheric exponent or the scale height for each layer. This array of numbers is computed by CURR_ATM (See Appendix 1) and is used by routines which specifically compute temperature and pressure as functions of altitude. Density calculation is not explicitly added but should be computed from the perfect gas law ($\rho = p/RT$).

If temperature data comes from aircraft aloft, then it should be recognized that the aircraft altitude will be a pressure altitude and not the geometric altitude required in the equations above. This can be

corrected by using the model atmosphere relations and the lower altitude temperature data to explicitly calculate the difference between geometric and pressure altitudes.

The coding for the current atmosphere routines is done as a script file in Matlab. The Matlab code is 'C-like' however and a conversion to 'C' or some other higher order language is relatively straight-forward. See Appendix 1 for a source listing of the routines available.

1.4.1 Note on Altimeter Settings

An aircraft altimeter is calibrated to read out an altitude above mean sea level based on the model atmosphere. There is an additional setting parameter however which allows the altimeter to deviate from this value. For safety of flight, when operating below 18,000ft, pilots are required to adjust their altimeters to a fictitious pressure broadcast by the local station. This fictitious 'corrected' pressure is such that at the physical ground level the altimeter reads the actual height above sea level for the local point in question. For commercial air traffic this generally corresponds to the airport, from which the aircraft is departing from, or arriving at. This corrected barometric pressure is entered manually by an adjustment screw on the altimeter and displayed in the 'Kollsman window' of the altimeter. In the United States, the Kollsman window is calibrated to inches of mercury. Nominal sea level pressure is 29.92 in Hg and this setting is always used when flying above 18,000ft. In general the atmosphere is not 'standard' and hence for an aircraft at the runway altitude, the altimeter will not read the posted runway altitude without some adjustment . The broadcast Kollsman window setting is simply a

fictitious pressure that rotates the altimeter dial so that a correctly calibrated altimeter reads correct runway height when the aircraft is on the runway. The physical interpretation of the Kollsman setting is shown in Figure 3, taken from Ref. 2. It is important to note that for a non-standard atmospheric pressure variation, the altimeter will read the correct geometric altitude only at the runway. At other altitudes the altitude must be corrected to obtain geometric altitude just as in the standard atmosphere case.

2. Wind modeling

Lack of accurate data on current atmospheric winds would be a serious impediment to the accurate predicting of aircraft arrival times at the runway and at various intermediate waypoints. While this would not pose a safety problem for the CTAS system, the lack of accurate winds would result in increased controller advisories, and a loss of aircraft efficiency due to the extra maneuvering required to maintain spacing and arrival rates. Fortunately there are several sources of wind data available which make wind profile generation feasible. Wind data is available from: (1)

Meteorological information available in the vicinity of most airports, (2)

Enroute information from inertially equipped aircraft, and (3) Wind data from the NOAA Wind Profiler network which is available (or soon will be) for 31 selected sites across the country.

Access to, and usage of, the NOAA Profiler system data is discussed extensively in the next few sections of this report. Data processing requirements for the other data types (items (1) and (2) above) is similar;

only the methods of data collection are different. In the current study, data collection for these data types has not been considered and is a topic for further research.

2.1 Wind data: NOAA Profiler system

The wind profiler system currently being implemented by the National Oceanic and Atmospheric Administration (NOAA) was designed with the primary goal of weather prediction, particularly to help model and predict thunderstorm activity in the central section of the United States. There are currently 31 sites planned. The locations of these sites are shown in Figure 4 and Table 2.1. For background on the Profiler system see Reference 3.

The physical setup for a typical profiler site is depicted on Figure 5. At the Profiler site three doppler radar beams are used. One beam is vertical, the other two are each 15 degrees from the vertical and oriented orthogonal to each other, preferably in the North and East directions, but generally skewed due to potential interference with aircraft and satellite communications. (See Table 2.1). Back scattering of the radar beam from particulates and small scale turbulence in the atmosphere allow determination of the radial wind velocity along the three beams as a function of altitude. The altitude dependency is separated out by sending out radar pulses and processing reflected radar returns as a function of the time delay. These three non-orthogonal velocity components can be transformed to give magnitude and heading of the horizontal component of the wind, which are available as outputs of the Profiler station, as well as a

vertical component (which is not available to external users.) For details on the operation of the Profiler, see Ref. 3.

The wave length of the radar determines the altitude resolution of the beam and its maximum altitude capability. Higher frequencies (hence shorter wave lengths) give better resolution but have a lower usable altitude range due to the lack of smaller scale turbulence at higher altitudes. The standard profiler site uses a frequency signal of 404 MHz ($\lambda \approx 70 \, \mathrm{cm}$), which can give data, up to about 60,000ft. This system is operated in a high resolution mode and a low resolution mode by varying the pulse width and the averaging interval. In the low resolution mode, winds can only be obtained up to about 35,000ft. There is an additional Profiler site at Denver Stapleton airport that is not part of the Profiler Network. While functioning quite similarly to the Profiler sites, this site is an experimental station and operates at a frequency of 915 MHz. Hence it provides more accurate data over a smaller altitude range, and as discussed later, is more sensitive to environmental conditions.).

At the time of this writing, only the station at Platteville, Colorado is available for data, although several other stations are currently operating in a test mode. The complete complement of 31 sites should be available by the end of 1991.

For use in wind prediction in the ATC problem, some knowledge of the data characteristics of this system are needed to aid in utilization of the data. Several factors can influence the quality of the received data. The primary adverse factor is precipitation. Since falling precipitation can produce a large return signal, any precipitation can seriously affect the quality of the data, particularly due to spatial inhomogeneities in droplet

1 3

speeds and distribution. This effect is especially true at higher radar frequencies, hence the Denver experimental facility frequently is most often affected by precipitation.

This effect is magnified if local inhomogeneities affect the different beams in different ways. In fact, local inhomogeneities of any type can cause discrepancies since the velocity transformations to compute horizontal velocity assume spatial homogeneity. Due to the beam deflection angles this means that at high altitudes, beam locations are several miles apart. The velocity calculation effectively requires differencing to remove the vertical wind component. Any spatial variation in vertical winds between the different beams will be translated into erroneous horizontal velocity components.

A third factor affecting the Profiler can be local changes in reflectivity of any type. For example the operation of the doppler radar is dependent on backscattering of the emitted beam from dust and density fluctuations in the air. The reflection is particularly sensitive to fluctuations whose length scale is half a wavelength. Particularly at high altitudes, inherent atmospheric stability and lack of turbulence can make the reflected signal extremely weak. In these cases backscattering from other sources in the side lobes of the radar can cause spurious reading.

At the radar site a number of separate averages is performed to determine wind speed components at each altitude. As part of the Profiler output the number of averages and the returned signal power is given as output data also. If insufficient averages are available, or the data fails a consistency check, the value '-999' is given for wind magnitude to indicate a bad data point. While the number of averages and the power value

should give some indication of data quality, our experience has been that this is a rather unreliable indicator. A better choice appears to be to view the data graphically, and to visually scan for bad data points. Data currently available at NASA Ames is for the Platteville and Denver sites. Typical data received from these stations is shown in Table 2.2.

Some Profiler stations will be equipped to report on additional surface conditions. In particular, the temperature and pressure are of interest for the ATC problem.

2.2 Wind Profile estimation

Typical wind versus altitude data is shown in Figure 6 for the Platteville and Denver reporting stations. This data needs to be further smoothed, and outlier points removed for a consistent trajectory prediction algorithm. Several types of assumptions on wind variation with altitude could be used. For our purposes we have assumed that the data is to be fit to a series of contiguous straight line segments of velocity versus altitude. The number of segments is variable and is an input from the analyst at the time the data is to be processed. Fitting is done through a weighted least squares algorithm, which is identical to the prediction phase of a Kalman filter. Data is fit independently for the North and East components of the wind. Note that since the Platteville site is aligned in the North-East direction, this is equivalent to smoothing the raw data directly. For other sites with a non-North-East orientation, estimation applied to the natural orientation of the site is probably preferable to

North-East. Note also that while the wind components each vary linearly with altitude, the magnitude and wind heading will not.

For a set of fixed altitude break points for the various segments the data is fit to the segments by the weighted least square algorithm. (see e.g. Bryson[3]) Generally for Profiler data, all data weights for all wind values are assumed to be the same. Outliers are generally explicitly removed from the data although a much reduced data weighting would have virtually the same effect. A few typical fits to the data are shown in Figure 7. If desired, the breakpoint altitudes can also be included as parameters in the data fit. This can lead to improvement in the data residuals, at the expense of more lengthy and possibly ill-conditioned computations. A typical fit with variable breakpoints is shown in Figure 8. Note while this case is well-behaved, the fitting process here is non-linear, and hence an iterative improvement process is required to produce a final fit. If initial points are chosen reasonably, in our experience this fitting process usually proceeds with little difficulty. With a poor initial guess however, this fit can, and has, diverged in some of our simulations. divergence in an operational scenario could be quite serious, some safeguards to prevent this would be necessary in an operational setup.

The details of the fitting procedure follow the standard least squares procedure. The Matlab code which has been developed to perform the fit for the Profiler data is given in Appendix 2. Note that in this code, we have added separate outlier logic which searches the fitted data for points which are significantly distant from the fit and automatically marks such data for deletion. In practice, this section worked quite well, and removed only those points which visually we felt to be outliers. Occasionally, if data

was particularly noisy and data residuals were high, then some points which visually appeared to be outliers were not detected by this algorithm. In such cases however, the entire Profiler wind data was often suspect, and consideration of other data types may be necessary.

2.3 Other Data types

Other wind data types should be available in an operational system. This will be necessary if the appropriate spatial resolution of the winds is to be determined, and will be necessary at sites not close to a wind profiler site. Such data is most likely data from inertially equipped aircraft, which can determine winds from the combination of air and inertial data. This data is currently available to the airlines- what is needed is a mechanism for obtaining this data for purposes of Air Traffic Control.

Data processing of additional data types is considered to be identical to that of the Profiler data. The only decision is to estimate the relative accuracy of the data so that the appropriate data weighting relative to the other data types can be established.

2.4 Spatial & temporal variation

Wind profiles can exhibit considerable spatial and temporal variation.

This variation must be accounted for and captured in a wind estimation strategy for CTAS. For example, a plot of some typical wind profiles measured at close time intervals at the Denver and Platteville profiler sites is shown in Figure 9. Similarly, overplots of the Denver and Platteville winds reported at the same times demonstrate the spatial

variability from the two sites (which are less than 50 mile apart). See Figure 10. Because of this, the wind models proposed must be dynamic. That is, it is anticipated that once sufficient data becomes available, a fully time varying, three dimensional wind profile should be the goal of this system. Looking at aircraft arriving on major jetways, the initial goal is to formulate separate wind profiles on major jetways. Temporal variations are included by appropriate filtering of past and current wind data. In particular, a Kalman filter structure with added process noise to fade out old data is a straight-forward and reliable way to ensure optimum usage of wind data. Specific filter design characteristics such as required process noise will need to be determined once real data is available.

3. Conclusion

This report summarizes the author's initial efforts toward formulation of a wind and atmospheric model for implementation into CTAS. A basic approach and set of algorithms has been developed for the wind and atmospheric estimation problems. Additional data types can easily be included in the estimation algorithm. Attention to the logistics of data collection is a significant problem to be addressed in the future to achieve the level of accuracy sought in the CTAS system.

References

- [1] U.S. Standard Atmosphere, 1962, US Government Printing Office.
- [2] Simonson, Leroy, Commercial Pilot Studyguide, Aviation Book Co., Glendale, CA.
- [3] , Wind Profiler, Training Manual, vols 1-5, National Weather Service, Office of Meteorology, August 1989.
- [4] Bryson, A., Ho, Y.C., <u>Applied Optimal Control and Estimation</u>, Halsted Press, J. Wiley & Sons, New York, 1975.

Table 2.1 Profiler sites

NOAA Wind Profiler Demonstration Network
Site Information - A
January 26, 1990

Site Orientation from True N $\binom{0}{1}$		1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -	110 111 110 110	116 116 120 120 110 110 100 100 100 100 100 100	-4- +1 0
Magnetic N Decln (', ')	0.04	00	- 10 70 W W P	07 00 01 29 00 01 29 00 05 08 03 58 09 51 09 38	4 D .
Elev. (ft.)	975 1420	1465 4016 2125 835 1005	695 1085 1280 1035	1720 557 640 1045 1045 1305 1305 2625 2625	3250 6551 6240
Long. (W)	10 20 20	17 20 05 38 28	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	97, 47, 37, 37, 39, 39, 39, 39, 39, 39, 39, 39, 39, 39	01 41 06 11 07 54
Lat. (N)	0 10 4	848846 848846	5 4 4 5 4 6 4 6 4 6 4 6 4 6 6 6 6 6 6 6	208028444118660	50 0 0 0 0 0 0
site ID	PLTC2 LTHM7 FBYN1	HBRK1 WSMN5 HVLK1 NDSK1 LMNO2	HKLO2 PRCO2 CNWM7 SLAI4	MLGNI WNCI2 WLCI3 WLCI3 BLMM7 SBYM3 WDLM5 OKOM6 WNFLI PATT2 JTNT2 TCUN5 GDAC2	MBWW4
Site No.	357	4 17 10 12 18 18	117 117 117 117 117	11111111111111111111111111111111111111	30 31
State	NAC	MR NW KS COK COK COK	M O O O S	M M M M M M M M M M M M M M M M M M M	M W W
Nearby Town	Platteville Lathrop Fairbury	Hillsboro White Sands M Haviland Neodesha Lamont	Haskell Purcell Conway Slater	Winchester Blue River Wolcott Bloomfield Maynard Wood Lake DeQueen Okolona Winnfield Palestine Jayton Tucumcari Granada Morriman	Medicine Bow Aztec

Profiler Program Office Contact: Margot Ackley Comm: 303/497-6791 FTS: 320-6791

Table 2.2 Raw data received from Denver/Platteville profiler

SITE: DENVER -- horizontal low mode WIND profile

DATE: 90/07/23

TIME: 20:00:00 (UTC) at start of acquisition period

PROFILES: 12 TIME DOMAIN AVGS: 124 SPECTRA: 10

PULSE WIDTH: 1.33 MICRO-SECS PULSE REP PERIOD: 50.00 MICRO-SECS

MAX HOR VEL: 51.05 M/S
FIRST HEIGHT: 289.78 M/AGL
DELTA HEIGHT: 193 METERS

HEIGHTS (GATES): 32

6185	SPEED	DIRECT			"	POWER	(EAST)
GATE	M/S	DGRS	KM/MSL	#E	#N	DB	
1	.9	306	1.90	11	9	65.2	С
2	2.8	83	2.09	9	7	77.5	С
3	4.1	39	2.29	11	6	71.0	С
4	.9	43	2.48	11	11	73.1	С
5	1.2	326	2.67	10	10	74.8	С
6	3.3	307	2.87	12	10	75.0	С
7	3.0		3.06	12		75.1	
8	6.0	302		12		67.3	
9	9.5	281		12	11	59.8	С
10	9.5	290	3.64	12	12		С
11	9.9	290	3.83	12	12		С
12	11.3	290	4.03	12	12	54.5	
13	11.9	298	4.22	12	12	50.3	
14	12.4	296	4.41	12	11	48.4	
15	11.6		4.61	12		55.3	
16	12.3		4.80	12			
17	12.3			12			
18	12.8			12		52.0	
19	13.4			12		49.2	
20	13.7		5.57	12	12	50.2	
21	14.1	301	5.76	12		49.9	
22	14.6	296	5.96	12	11	50.5	
23	14.1	297	6.15	12	10	46.9	
24	14.7	299	6.34	12	10	48.0	
25	15.7	309	6.54	11	11	51.5	
26	17.1	306	6.73	12	12	45.7	С
27	18.1	302	6.92	12	12	43.0	С
28	18.3	304	7.12	12	12	37.1	
29	18.5	304	7.31	11	12		С
30	18.5	309	7.50	11	12	41.9	
31	18.4	310	7.70	12	12	43.4	
32	18.1	315	7.89	11	12	41.1	С

SITE: PLATTEVILLE -- horizontal low mode WIND profile

DATE: 90/07/23

TIME: 20:00:00 (UTC) at start of acquisition period

PROFILES: 12 TIME DOMAIN AVGS: 350 SPECTRA: 8

PULSE WIDTH: 3.67 MICRO-SECS PULSE REP PERIOD: 238.00 MICRO-SECS

MAX HOR VEL: 69.81 M/S

Table 2.2 Raw data received from Denver/Platteville profiler(cont)

FIRST HEIGHT: 1786.96 M/AGL DELTA HEIGHT: 289 METERS

HEIGHTS (GATES): 24

GATE	SPEED M/S	DIRECT DGRS	HEIGHT KM/MSL		#N	POWER DB	(EAST)
1	2.8	91	3.31	10	12	61.1	
2	1.4	323	3.60	11	11	61.5	
3	4.7	290	3.89	12	11	58.2	
4	8.8	297	4.18	12	11	62.6	
5	11.1	298	4.47	12	11	65.7	
6	12.2	296	4.76	12	12	66.8	
7	12.8	295	5.05	12	12	66.1	
8	13.1	296	5.34	12	12	65.2	
9	13.3	298	5.63	12	11	66.4	
10	13.4	303	5.92	12	11	68.5	
11	13.4	304	6.21	12	11	67.5	
12	13.2	306	6.50	12	12	62.4	
13	14.3	305	6.79	12	12	55.9	
14	16.3	302	7.08	12	11	50.2	
15	15.4	307	7.37	12	12	47.6	
16	15.4	313	7.66	12	12	50.1	
17	16.2	314	7.95	12	10	49.1	
18	18.9	309	8.24	11	10	47.5	
19	19.3	308	8.53	11	8	44.9	
20	20.9	306	8.82	11	8	40.3	
21	19.8	300	9.11	12	11	38.9	
22	20.1	293	9.40	12	12	40.5	
23	20.6	290	9.69	12	11	39.5	
24	21.1	292	9.98	12	10	33.7	

SITE: PLATTEVILLE -- horizontal high mode WIND profile

DATE: 90/07/23

TIME: 20:00:00 (UTC) at start of acquisition period

PROFILES: 12 TIME DOMAIN AVGS: 124 SPECTRA: 16

9.67 MICRO-SECS PULSE WIDTH: PULSE REP PERIOD: 672.00 MICRO-SECS

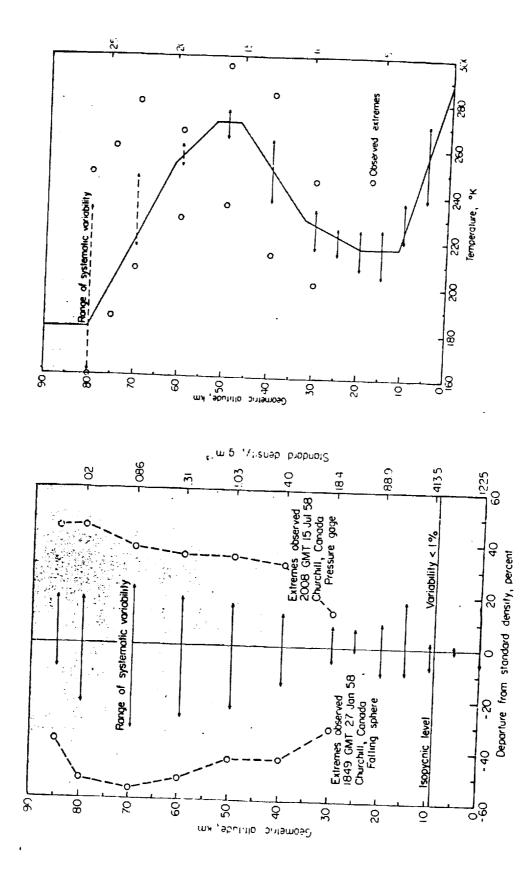
DELTA HEIGHT: 4201.77 M/AGL
HEIGHTS (GT MAX HOR VEL: 69.78 M/S 869 METERS

HEIGHTS (GATES): 16

GATE	SPEED M/S	DIRECT DGRS	HEIGHT KM/MSL		#N	POWER DB	(EAST)
1	13.3	302	5.73	12	11	71.8	
2	13.7	304	6.59	12	11	67.8	
3	15.0	308	7.46	11	11	55.6	
4	16.7	311	8.33	11	12	51.0	
5	18.9	298	9.20	12	11	44.6	
6	20.7	294	10.07	11	10	40.2	
7	22.8	292	10.94	10	8	35.6	
8	23.2	293	11.81	11	10	36.5	
9	23.7	285	12.68	11	9	39.6	
10	21.8	285	13.55	11	9	39.8	
11	19.5	282	14.42	12	10	33.9	

Table 2.2 Raw data received from Denver/Platteville profiler(cont)

12	13.2	303	15.29	11	7	31.0
13	9.3	321	16.16	7	11	29.9
14	4.3	261	17.03	7	10	26.6
15	6.6	279	17.90	4	5	25.5
16	-999.0	-999	18.77	5	3	27.5



- · - :

Figure 1 Statistical Variation of Atmospheric Parameters

Figure 2 Temperature deviation from standard and the induced altitude errors.

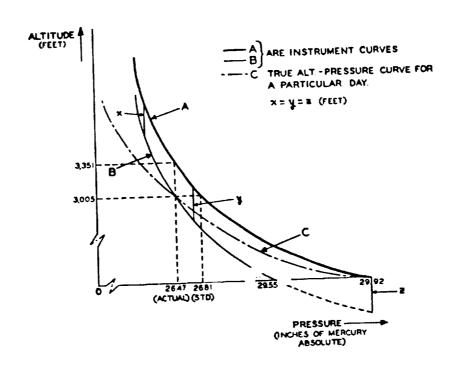


Figure 3 Explanation of the Kollsman window setting.

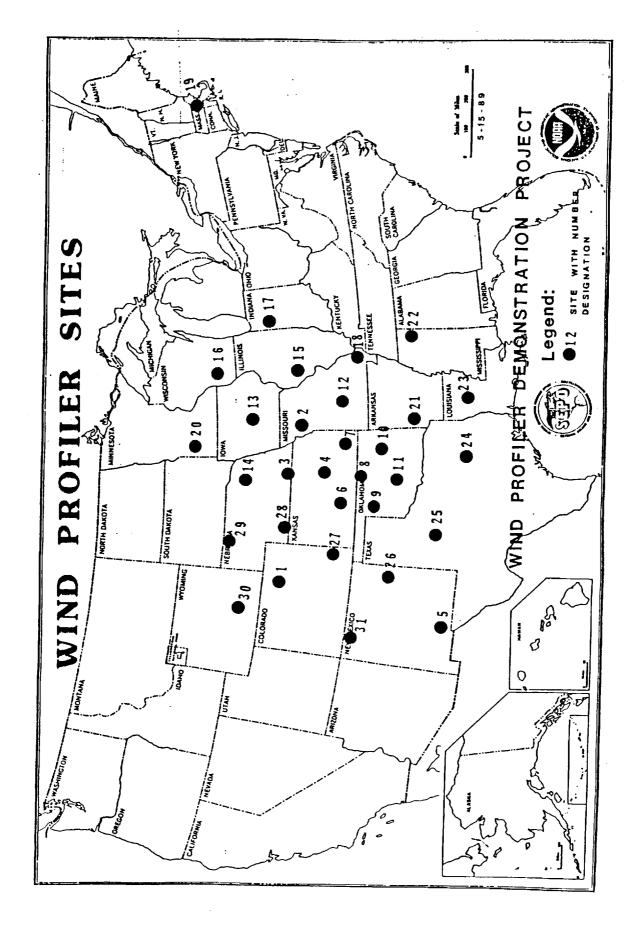


Figure 4 Profiler sites across the United States.

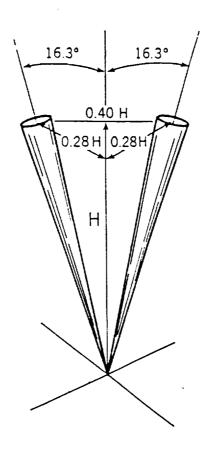


Figure 5 Geometry of a Profiler Radar beam.

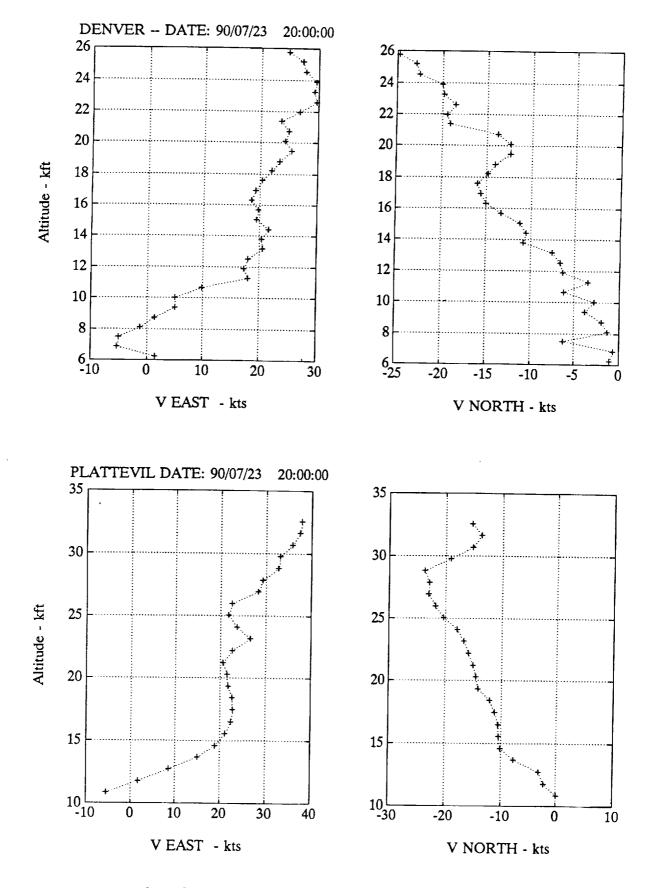
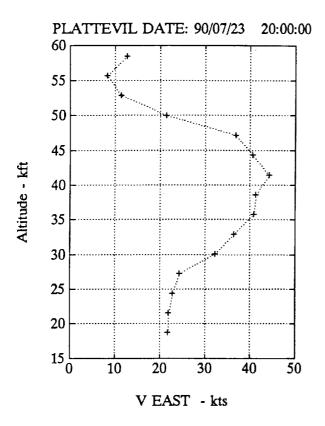
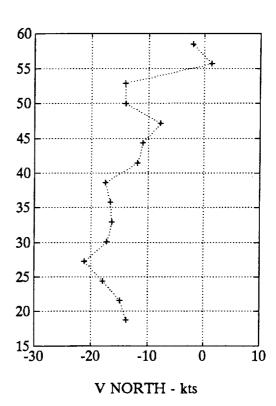
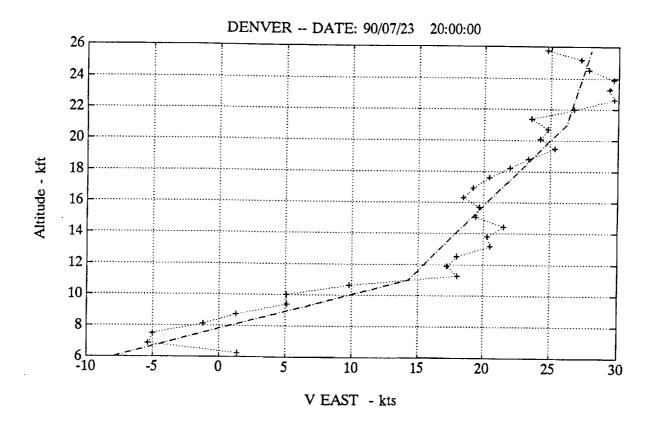


Figure 6 On-line data from Denver-Platteville Profiler site.







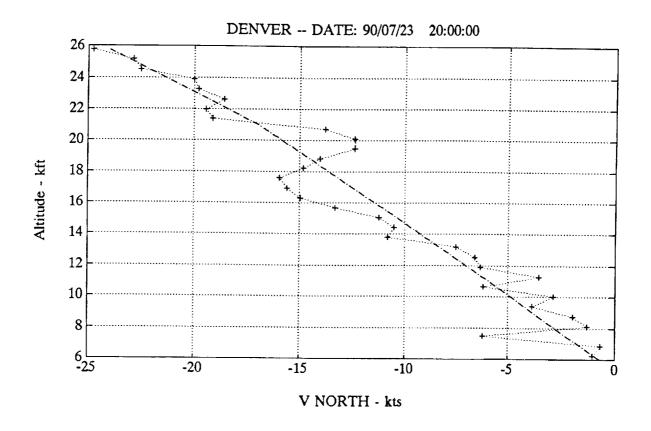


Figure 7 Typical straight line fits to Profiler wind data.

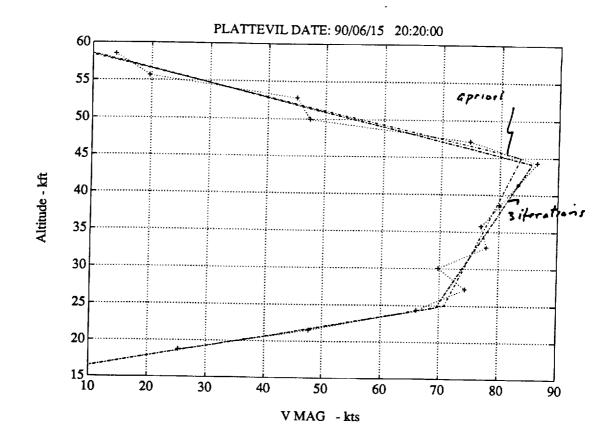


Figure 8 Fit to Profiler data showing iteration of variable breakpoints.

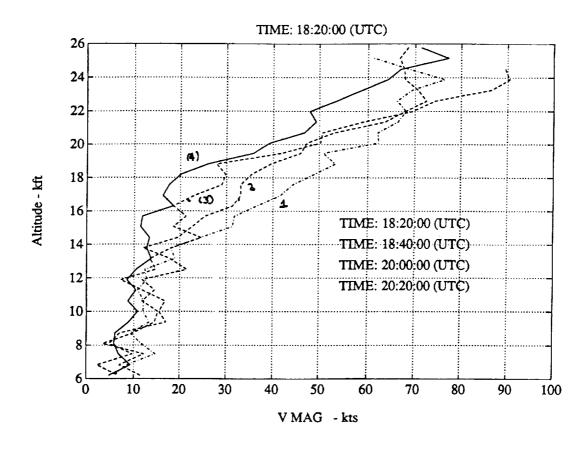
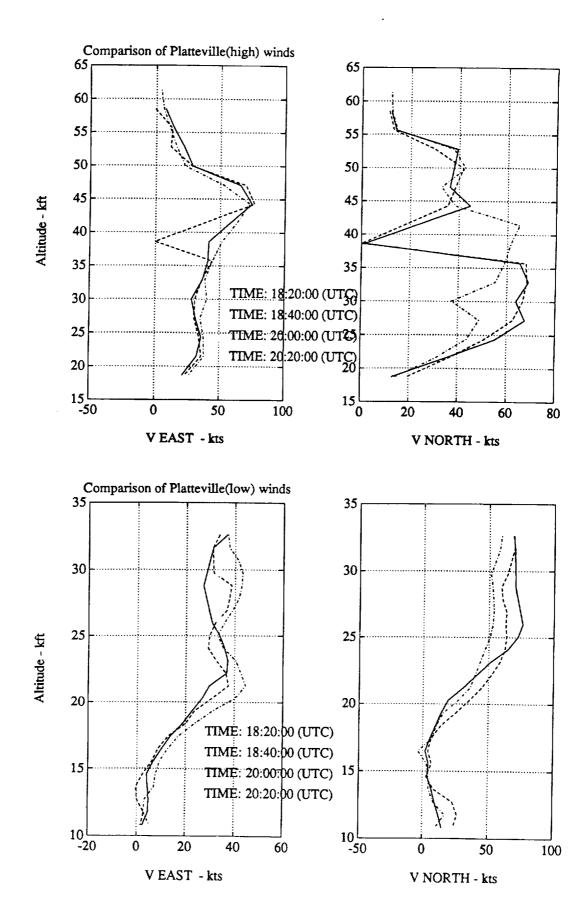


Figure 9 Temporal variation of winds at Denver



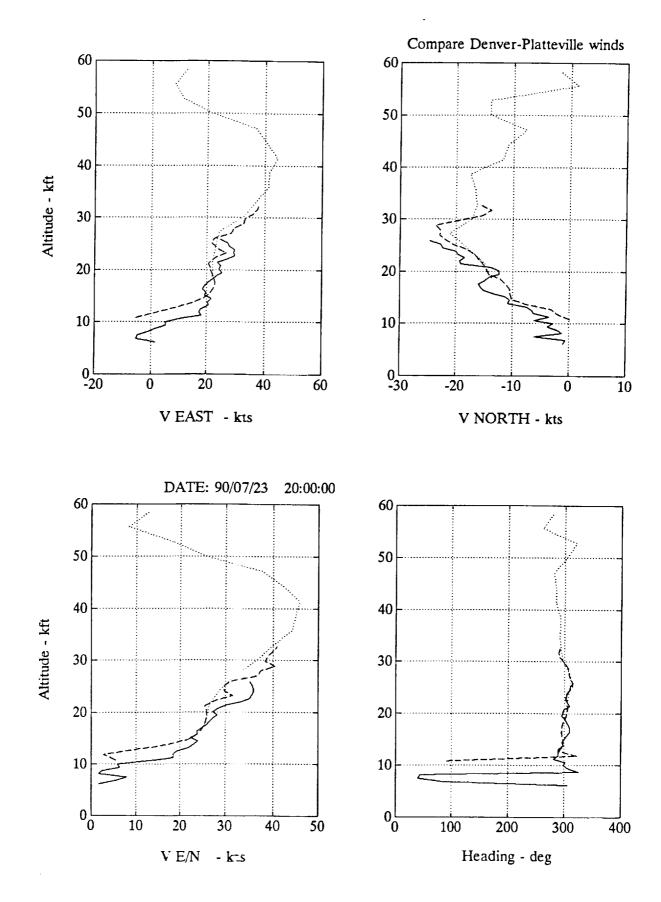


Figure 10 Comparison of winds at Denver and Platteville sites showing spatial variation.

APPENDIX A

```
XNASA Ames atmospheric routines (Matlab code)
       contains:
                 curr_atm.m : Generates atmosphere from temperature data
                 inter.m
                             : Interpolatioon utility
                 pres_alt.m : Return pressure altitude given h
                 pressure.m : Return pressure (uses curr_atm) given h
                             : Returns altimeter reading given pressure
                 rd alt.m
                 ttempf.m
                             : Returns temperature given h
                 value.m
                             : Interpolation utility
 % curr atm.m
                  gls 8/29/90
 %Program to generate a matrix of current atmosphere parameters
     to determine pressure, density, temperature as functions of
     geopotential altitude. Output is matrix ATM defined by
 %
     ATM=[tempf;
                    %Input row vector of temperature (deg R)
 %
          alt;
                    %Input row vector of altitude (ft)
%
                    20utput row vector of pressure (pres0(1) input)
          pres0;
ኧ
          alph;
                    %Output lapse rate between alt(i)-alt(i+1)/Hs at last pt
Z
         nexp];
                    %Pressure exponent or scale height if alph==0
%
    Used by function Pressure
    The current temperature, altitude data points are fixed here.
    Change to read from a file if desired
%N.B. HERE input tempf is deg F--output is deg R
tempf=[100 80 -69.7]:
alt=[0 5000 36089];
p0=1013.25;
%THIS IS THE STANDARD ATMOSPHERE
%tempf=[59 41.169 -69.7]; %temp deg F for altitudes in h
%alt= 1000*[0 5 36.089]; %altitude in thousands of ft
%p0= 1013.25; % pressure at h0
% INTERNAL variables are all metric for easy reference
cm2f = 1/.3048; %meter to ft EXACT
g0 = 9.80665; R = 1000*8.31432/28.9644;
conv= 1.8/cm2f; % deg K/m to deg R/ft
gqR = conv*g0/R; % units now deg R/ft
cN2p = 1/(0.45359237*g0); %Newtons to pounds
tref= 1.8*273.15 -32; % 0 deg F
               %tolerance for "0" lapse rate
eps = 1.e-7;
% end setup
LL= length(tempf);
% Form an array of lapse rates, exponents and pressures
% assume isothermal above last temperature given
pres0(1) = p0;
for ii=1:LL-1
  alph(ii) = (tempf(ii+1) - tempf(ii))/(alt(ii+1) - alt(ii));
  if abs( alph(ii)) > eps;
```

```
nexp(ii) = -gqR/alph(ii);
     presO(ii+1) = presO(ii)*((tref+tempf(ii+1))/(tref+tempf(ii)))^nexp(ii);
   else
      nexp(ii) = (tempf(ii) +tref)/gqR; %this is scale height
      presO(ii+1) = presO(ii)*exp(-(alt(ii+1) - alt(ii))/nexp(ii));
     end;
end: %for
alph(LL) = 0;
nexp(LL) = (tempf(LL) +tref)/gqR; %this is scale height
for ii=1:LL, tempf(ii)= tempf(ii)+tref;end;
ATM=[tempf;alt;pres0;alph;nexp];
Ifunction to return interpolation indices for one dimensional array
    See function value to return interpolated value
%function zzz = inter(h,harray)
   returns zzz=[iref,a] such that
   h = (1-a)*harray(iref) + a*harray(iref+1);
ጄ
   iref = 0 if h < harray(1)
   iref = -1 if h > harray(max)
%
         and a= h - harray(max)
ኧ
   gls 8/23/90
function zzz = inter(h,harray)
[nr,nc]=size(harray);
if min([nr,nc]) --1
  Ll=max([nr,nc]);
else disp('Not a 1-d array'); return
end;
if h>=harray(L1)
   iref=L1; a= h-harray(L1);
elseif h<harray(1),
   iref=0; a= h-harray(1);
else
   stop=0; i=2;
   while stop=0;
      if h<harray(i)</pre>
          iref=i-1;
          a = (h - harray(iref))/(harray(iref+1)-harray(iref) );
          stop=1;
      else i=i+l;
      end;
   end;
end:
zzz=[iref, a];
% function to return pressure altitude for a given pressure
  altpres = pres alt(press); OR pres alt(press, str) str='mb' or 'hg'
```

```
uses English units (ft, psf) unless mb - milibars
 %
 Z
                                            or hg - in hg specified
   INTERNAL variables are all metric for easy reference
 % Use the NASA (ICAO) standard atmosphere
 %function altpres = pres_alt(press,str);
 function altpres = pres_alt(press,str);
 cm2f = 1/.3048; %meter to ft EXACT
 g0 = 9.80665; R = 1000*8.31432/28.9644;
 gqR = g0/R;
 alphstd= -.0065;
htropo = 11000;
tempstd= 288.15; %15deg C
t_tropo= tempstd + alphstd*htropo;
hscale = R*t_tropo/g0;
pstd= 1013.25; %millibars
cN2p = 1/(0.45359237*g0); %Newtons to pounds
pstdE = 100*pstd*cN2p/(cm2f^2);
                %pstdE= 2116.2; %English units (psf)
M2E= pstdE/pstd;
p_tropo = pstd*(t_tropo/tempstd)^(-gqR/alphstd);
% end setup
if nargin ==2
    if str=='mb', disp('mb')
    elseif str=='hg', press = press*pstd/29.9213;disp('hg')
else press = press/M2E;
end:
if press > p_tropo
      altpres = (tempstd/alphstd)*( (press/pstd)^(-alphstd/gqR) - 1);
     altpres = htropo + hscale*log(p_tropo/press);
else
end:
altpres=cm2f*altpres; %remove this to return in meters
**************************
% Given a temperature profile, generate pressure vs. altitude
% Assume linear temperature profile between points
ኧ
    function press = pressure(alt,ATM)
     alt in "ft"; pressure in "mb"
    Matrix ATM generated by curr_atm.m contains current atmosphere model
% Uses functions inter.m and value.m to get table values
function press= pressure(alt,ATM)
temp0= ATM(1,:);
harray=ATM(2,:);
press0=ATM(3,:);
alph=ATM(4,:);
```

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```
nexp=ATM(5,:);
zzz= inter(alt,harray);
iref=zzz(1); a=zzz(2);
temph= value(temp0,zzz);
if alph(iref) ~=0
   press= press0(iref)*(temph/temp0(iref))^nexp(iref);
else press = press0(iref)*exp(-(alt - harray(iref))/nexp(iref));
end:
% function to return altimeter reading for a given pressure
  altpres = rd_alt(press,kollsman); OR rd_alt(press,kollsman,str) str='mb' or
'hg'
            press is the current pressure
%
                English units (psf) unless mb - milibars
Х
                                       or hg - in hg specified
            kollsman is the altimeter setting (kollsman window)
X
              assumed in in Hg unless str='mb' --> then in mb also
2
            altpres is in (ft)
  Use function pres_alt.m which uses
ሄ
  the NASA (ICAO) standard atmosphere
%function altpres = rd_alt(press,kollsman,str);
function altpres = rd_alt(press,kollsman,str);
% function
if nargin --- 3
   if str=='mb',
      h1=pres_alt(press,'mb');
      h2=pres alt(kollsman,'mb');
      altpres= h1 -h2;
   elseif str--'hg',
      hl=pres_alt(press,'hg');
      h2=pres_alt(kol1sman,'hg');
      altpres= h1 -h2;
elseif nargin==1, kollsman=29.92;
end;
if nargin<3,
  h1= pres_alt(press);
  h2= pres_alt(kollsman, 'hg');
  altpres=h1-h2;
end;
```

 ${\it X}$ Given a temperature profile return temperature for a given h

```
% Assume linear temperature profile between points
    function temp=ttempf(h,ATM)
     h is alt in "ft"
    Matrix ATM generated by curr_atm.m contains current atmosphere model
% Uses functions inter.m and value.m to get table values
function ttemp= ttempf(h,ATM)
temp0= ATM(1,:);
harray=ATM(2,:);
zzz= inter(h,harray);
iref=zzz(1); a=zzz(2);
ttemp= value(temp0,zzz);
*************************
    function to return function value using linear interpolation
    on one dimensional array.
    Input are interpolation indices
    See function value to return interpolated value
    function h= value(harray,[iref, a])
2
    [iref,a] returned from inter.m such that
   h = (1-a)*harray(iref) + a*harray(iref+1);
ኧ
ጄ
   iref = 0 if h < harray(1)</pre>
          returns h-harray(1)
ሂ
    iref = max if h > harray(max)
          returns h-harray(max)
    gls 8/23/90
function h = value(harray,zz)
iref=zz(1); a=zz(2);
[nr,nc]=size(harray);
if min([nr,nc]) -1
  L1=max([nr,nc]);
else disp('Not a 1-d array'); return
end;
if iref<=0
  h=harray(1);
elseif iref-Ll
  h= harray(iref);
else
  h = (1-a)*harray(iref) + a*harray(iref+1);
end;
```

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APPENDIX B

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```
%NASA Ames routines for wind profile fit (Matlab code)
       contains:
                wnd7.m
                           : Read Profiler data and plot
                fit7.m
                           : Least squares fit to data
                             both these current versions are hardwired
                             to eliminate options available in early code
***********************
% wnd7.m 8/22/90 Master in /matlab/gls ALL Plat mod
%test wind profile
%load wind profile from data file
disp('Data should be loaded in standard format')
PLAT- 'PLAT'; DENV-'DENV';
El=exist('txtla'); wherl='
E2-exist('txt2a'); wher2-' ';
E3=exist('txt3a'); wher3=' ';
nam=[ 'V EAST '
      'V NORTH'
      'V MAG
      'V E/N '];
disp(' Plot data for')
if E1, wher1 = txtla(7:10); disp(['1: 'txtla]); end;
if E2, wher2 = txt2a(7:10); disp(['2: 'txt2a]); end;
if E3, wher3 = txt3a(7:10); disp(['3:'txt3a]); end;
disp([' 4: ' 'Platt.- ALL']);end;
disp('')
numin= input('
                   -->');
if numin-4, %this finds the Plattville data--IF IT EXISTS--
  plat1=0;plat2=0;
  allplat-1;
  if wherl---PLAT, plat1=1; numin=1;
  end;
  if wher2-PLAT,
         if plat1--1, plat2-2;
         else plat1=2; numin=2;
         end;
  end;
  if wher3 -- PLAT,
          if plat1>0, plat2=3;
          else plat1=3;numin=3;
          end;
  end;
else allplat=0;
end; %numin--4
data= eval( ['data' num2str(numin)]);
txta= eval(['txt' num2str(numin) 'a']);
txta=[txta(7:15) ' ' txtb(1:15) ' ' txtc(6:14)]:
```

```
if allplat,
        [lowlen,temp] = size(data); %Save this for future use in fit
        data= [data;eval(['data' num2str(plat2)])];
        txta=[txta(1:15) '-ALL' txta(16:35)];
        numin = 4;
        [hilen,temp]=size(data);
 end;
disp(' ')
% EAST & NORTH winds only
iplt=0;
   vmps= data(:,2);
   degs= data(:,3);
   altkm=data(:,4);
cd2r = pi/180.;
cm2f = 39.2/12;
cfps2kt= 1/1.69;
% make invalid data to nan
LL = length(vmps)
for ii=1:LL
   if vmps(ii) < 0,
      degs(ii)=nan; vmps(ii)= nan;
   end;
end; %ii loop
vxfps= -cm2f*vmps.*sin(cd2r*degs);
vyfps= -cm2f*vmps.*cos(cd2r*degs);
altkft= cm2f*altkm;
vplot= cfps2kt*vxfps;
vplot2= cfps2kt*vyfps;
% make sure hold is off and screen is clear
hold off
clg
subplot(121); % Do multiple plots
   if allplat,
      plot(vplot,altkft,'+');hold
      plot(vplot(1:lowlen),altkft(1:lowlen),':');
      plot(vplot(lowlen+1:hilen),altkft(lowlen+1:hilen),':');
    else plot(vplot,altkft,':',vplot,altkft,'+');
    end;
title(txta);grid;
xlabel([nam(1,:) ' - kts']); ylabel('Altitude - kft');
   lftaxis=axis; axis; %capture axes then release
   hold off
  if allplat,
      subplot(122)
      plot(vplot2, altkft, '+'); hold;
      plot(vplot2(1:lowlen),altkft(1:lowlen),':');
      plot(vplot2(lowlen+1:hilen),altkft(lowlen+1:hilen),':');
  else plot(vplot2,altkft,':',vplot2,altkft,'+');
 xlabel([nam(2,:) ' - kts']);
```

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```
grid;
 rgtaxis-axis; %capture axes then release
 %[xc,yc]=ginput(1,'sc');
 %text(xc,yc,txtb,'sc')
 %text(xc,yc+.05,txtc,'sc')
 hold on
 disp('do auto fit')
 fit7
 ******************************
 %fit7.m
 % fit wind data to best straight line segments using least square fit
 % Break points for altitudes are variable in this version
 % and number of segments are fixed.s
 % See fit1.m for f\bar{i}xed break points.
   8/19/90 mod for fit7.m in iter-1 only remove outliers automatically
           if fitted data point is very far out of bounds
 % gls 6/18/90 mod to fit4 7/18/90 for fixed or variable
 \frac{2}{6} 6/19/90 add for fit on subplots -->fit5.m
 % 6/20/90 add weighted ls + add other vel. data
% keyboard command disabled due to problems on SUN's
 sigls=1;
            %Covariance of basic wind data
 sig2s=.01; %Covariance of "added" data
 epsp= 1.e-3; parmchg=1;
hseg1=[ 25.0]; %altitudes in kft
hMAX = 1000;
disp('This program will fit straight lines to standard data')
disp('Assume equal noise covariance of sigls=')
disp(sigls)
disp('It will also pick up additional data from arrays')
disp('VEAST VNORTH HNEW if EXISTNEW is a defined variable')
disp('This data has covariance sig2s=')
disp(sig2s)
disp('Assume for this case data is plotted in E/N form')
itermax=10 %fixed for now
disp('itermax=l for fixed breakpoints');
disp(' ')
itermax=input('itermax= ')
disp('Determine least squares fit')
disp(' to straight line wind profile segments')
hsegl=input('Input initial breakpoint vector: ');
nsegs= length(hseg1)+1;
nparm= nsegs+1;
NEWDATA - exist('EXISTNEW'); %NEWDATA-1 if data
if NEWDATA, lnewdata= length(VEAST);end;
%number of parameters (per curve)in fit (exclude breakpoints!)
if iplt==0 | iplt==4, nparm2=nparm;
  else nparm2=0;end;
nparmt= nparm+nparm2;
%Get rid of nan's in data (+ outliers marked as nan)
```

```
LL= vplot~=nan;
vfit=vplot(LL);
h= altkft(LL);
% Make sure its a column vector
[nr,nc]=size(vfit); if nr==1 vfit= vfit';end;
[nr,nc]=size(h); if nr=1 h = h';end;
if NEWDATA, vfit=[vfit; VEAST]; h=[h; HNEW]; end;
     %if subplots, alt data string is same on both
if nparm2 > 0, vfit2=vplot2(LL); h2=h;
    if NEWDATA, vfit2=[vfit2;VNORTH];end;
    vfitt=[vfit;vfit2];ht=[h;h2];
 else vfitt=vfit; ht=h; end;
onevec=ones(vfit);
onevect= ones(vfitt);
% now work with only reduced data
lvel= length(vfit);
lold- lvel- lnewdata;
iter = 1;
   Enter main loopsize(
while parmchg > epsp %loop over estimator until convergence is met
  hseg= [ 0 hseg1 hMAX]; %segment boundaries
  A= zeros(lvel,nparm);
  A(:,1)=ones(vfit);
  L0= h > hseg(1)*onevec;
  for jcol=2:nsegs+1
    L1= h > hseg(jcol)*onevec;
    L01 = L0 - L1;
    A(:,jcol) = hseg(jcol)*L1 - hseg(jcol-1)*L0 + h.*L01;
    L0 - L1;
  end; %for jcol
  if nparm2 > 0,
      zA = 0*A;
      A= [A zA; zA A]; ht=[h;h];
  else ht=h; end;
 % Now add columns for breakponts
     but only in the second and higher iteration
  if iter -1, oldparm-zeros(nparmt.1):
  else %for iterations above 1, estimate break points
    A12= zeros(lvel,nsegs-1); A22= A12;
    for jcol=2:nsegs
       L1= h > hseg(jcol)*onevec;
       A12(:,jcol-1) = (parm(jcol) - parm(jcol+1))*L1;
     end; %for jcol
     if nparm2 > 0
       for jcol=2:nsegs
         L1= h > hseg(jcol)*onevec;
         A22(:,jcol-1) = (parm(nparm +jcol) - parm(nparm+jcol+1) )*L1;
       end; %for jcol
    A12 = [A12; A22];
    end; %nparm2
```

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```
A = [A A12];
     if iter==2, oldparm=[parm; hseg(2:nsegs)'];
        else oldparm = parm;
     end;
  end; %if iter
  Vfit= A(:,1:nparmt)*oldparm(1:nparmt); %Estimated measurements
  RIA-A:
  if NEWDATA.
     for irow=1:lold,
            RIA(irow,:)= RIA(irow,:)/sigls;
            RIA(lvel+irow,:)= RIA(lvel+irow,:)/sigls;
            end;
     for irow=lold+1:lvel;
            RIA(irow,:)= RIA(irow,:)/sig2s;
            RIA(lvel+irow,:)= RIA(lvel+irow,:)/sig2s;
            end;
  end; %if NEWDATA
 Api = inv(A'*RIA)*RIA';
 dparm=Api*( vfitt - Vfit);
 parmchg= sqrt(dparm'*dparm);
 parm- dparm+oldparm:
%Get new residuals for test
 Vfit= A(:,1:nparmt)*parm(1:nparmt); %Estimated measurements
  delv = ( vfitt - Vfit);
 rmsdv = sqrt( delv'*delv/length(delv));
 maxdelv= max( abs(delv) );
 disp(['RMS fit deviation = ' num2str(rmsdv) ' kts'])
 disp(['MAX fit deviation = ' num2str(maxdelv) ' kts'])
% Check velocity deviations here on first iteration
% auto delete outliers
  if iter -- 1
      rmst= max([rmsdv 2.5]); %Use 4*rms or 10 as outlier test
    Lol= abs(delv) > 4*rmst*onevect;
     lLol- Lol'*Lol; %this dot product gives the number of outliers
     if lLol - 0, disp('NO OUTLIERS FOUND')
      else
            disp([ num2str(lLol) ' OUTLIERS LOCATED AT alt='])
            disp(ht(Lol))
            %autodelete outlier--tricky logic as we will have to delete
            %data from both sets if E/N data being used
            if nparm2 > 0
                 Lol1= Lol(1:1vel); Lol2= Lol(1vel+1:2*1vel);
                 Loll = Loll + (Lol2 > Loll);
                 Lo12 = Lo12 + (Lo11 > Lo12);
                 Lol1 - onevec - Lol1;
                 Lol2 = onevec - Lol2; %Here Lol1 & Lol2 should be the same!
                 Lol = [Lol1; Lol2];
                 %Now get rid of outlier
                 vfitt= vfitt(Lol); h=h(Lol1);
                 vfit=vfit(Lol1); vfit2= vfit2(Lol2);
            else
                Lol = onevec - Lol;
                vfitt= vfitt(Lol);
                vfit= vfit(Lol); h= h(Lol);
```

: :

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end;%nparm2
           iter = 0; %final step- set iter back so iter=1 done again
           onevect = ones(vfitt);
           onevec=ones(vfit);
           lvel- length(vfit); %****NOTE ASSUME FOR NOW DELETED DATA WAS IN
OLDDATA SET
    end;%if lLol
  end; %if iter-1
    if iter > 0 disp('Estimated parameters:')
2
                disp(parm)
%
        end;
   if iter >1, hseg1= parm(nparmt+1:nparmt+nsegs-1)';
       end;
   iter= iter+1;
   oldparm- parm;
status=[ iter, parmchg,hseg1]; %display output
disp(status)
  if iter >itermax
     disp('--quit');
     parmchg =- parmchg; end; %if itermax
end; %while loop
% converged or quit. Now plot fit
htt= max( h );
hplot=[0 hseg1 htt]; %plot breakpoints and last point
vfit=[parm(1)];
for ii-2:nparm
  vfit(ii)= vfit(ii-1) + parm(ii)*(hplot(ii) - hplot(ii-1) );
end:
hold on
if nparm2 > 0,
  subplot(121);axis(lftaxis);plot(vfit,hplot,'b')
 vfit2=[parm(nparm+1)];
 for ii=2:nparm
   vfit2(ii)= vfit2(ii-1) + parm(nparm+ii)*(hplot(ii) - hplot(ii-1) );
 subplot(122);axis(rgtaxis);
 plot(vfit2,hplot,'b')
else plot(vfit,hplot,'b')
disp('End of fit7.m')
end % fit program
```